Symmetry of Magnetic Quantum Tunneling in Single Molecule Magnet Mn12-Acetate

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The symmetry of magnetic quantum tunneling has been studied in the prototype single molecule magnet Mn12-acetate using a micro-Hall effect magnetometer and superconducting high field vector magnet system. An average crystal fourfold symmetry is shown to be due to local molecular environments of twofold symmetry that are rotated by 90° with respect to one another, confirming that disorder which lowers the molecule symmetry is as important to magnetic quantum tunneling. We have studied a subset of these lower (twofold) site symmetry molecules and present evidence for a Berry phase effect consistent with a local twofold symmetry.

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Magnetic quantum tunneling (MQT) in molecules is a very active area of research, starting with the initial observations of resonant quantum tunneling in single molecule magnet (SMM) Mn12-acetate [1,2]. Quantum tunneling enables the creation of superposition states necessary for quantum computing and is also a mechanism for the loss of information in classical magnetic information storage. Condensed matter systems like these [3,4], with discrete energy levels coupled to the environment in the solid, are also important to understanding the border between quantum and classical physics, and the decoherence of quantum systems [5]. The symmetry of the molecule is the first step in understanding its energy level structure and quantum tunneling. For example, the symmetry determines the allowed terms in the spin Hamiltonian and, in particular, the form of the transverse interactions that lead to tunneling. However, in Mn12 as well as other SMMs MQT does not reflect the molecule site symmetry and the origin of tunneling has been an open question [6–19].

Mn12-acetate [Mn12(O2)(CH2COO)16(H2O)4]-2CH3COOH·4H2O consists of a core of 12 manganese atoms with a ground state spin of 10. The spin Hamiltonian of an ideal (S4-symmetry) Mn12-acetate molecule is

\[ H = -D S_z^2 - B S_z^4 + C (S_z^4 + S_z^4) - g \mu_B H \cdot S. \]  

The first two terms represent the uniaxial magnetic anisotropy of the molecule (D > 0 and B > 0). The parameters, \( D = 0.548 \) K, \( B = 1.1 \times 10^{-3} \) K, and \( C = 3 \times 10^{-5} \) K, have been determined by inelastic neutron spectroscopy [11] and EPR [12] experiments. There are thus \( 2S + 1 = 21 \) allowed projections of the spin on the z axis, with up and down projections along the z axis separated by an anisotropy barrier of \( \sim D S_z^2 + B S_z^4 \) (\( \sim 66 \) K). An applied longitudinal magnetic field, \( H_z \), shifts the energy levels favoring the projections of the magnetization parallel to the field direction. There are values of the \( z \)-axis field (resonance fields) for which the levels \( m \) and \( m' \) with antiparallel projections on the \( z \) axis are nearly degenerate, \( H_z \sim kD/g \mu_B \), \( k = m + m' \) (\( k \approx 44 \) T) and transitions across the energy barrier can occur. Interactions that break the axial symmetry and mix the levels \( m \) and \( m' \) lead to an energy difference between symmetric and antisymmetric linear combinations of spin projections known as the tunnel splitting. The lowest order transverse term allowed by the tetragonal symmetry is fourth order [i.e., the third term in Eq. (1)] and would lead to the tunneling selection rule \( m - m' = 4i \), with \( i \) an integer.

This is not observed experimentally. In addition, recent experiments show that there is a distribution of tunneling splittings in Mn12 crystals [16,17] associated with disorder. Two distinct models of disorder have been proposed. Chudnovsky and Garanin [14] proposed that random line dislocations in a crystal lead, via magnetoelastic interactions, to a lower molecule symmetry and a broad distribution of tunneling rates. Subsequent magnetic relaxation experiments indeed showed the existence of a broad distribution of tunneling rates and were analyzed in terms of this model [16,17]. In contrast, Cornia et al. [15] suggested, based on detailed x-ray analysis, that variations in the position of the two hydrogen-bonded acetic acid molecules surrounding the Mn12 clusters lead to a discrete set of isomers with lower symmetry than tetragonal. Our recent magnetic relaxation experiments in a longitudinal (easy axis) magnetic field are consistent with solvent disorder [18]. However, direct evidence of lower symmetry molecular environments in MQT experiments was lacking.

In this Letter we present studies of the symmetry of the magnetic response in deuterated Mn12 single crystals in the pure quantum regime (\( T = 0.6 \) K), in which relaxation is by MQT without thermal activation [10,20]. An average fourfold symmetry is unambiguously shown to be due to local molecular environments of twofold symmetry that are rotated by 90° with respect to one another, in accord with the model proposed by Cornia [15]. Further, we have studied a subset of these lower site symmetry...
molecules and present evidence for a Berry phase effect consistent with a local lower (twofold) symmetry.

The magnetization component parallel to the axial direction (z axis) of a Mn$_{12}$-acetate single crystal was measured using a high sensitivity micro-Hall effect magnetometer in a low temperature helium 3 system [21]. A single crystal was placed with one of its faces parallel to the plane of the sensor while a high field superconducting vector field magnet was used to apply magnetic fields at arbitrary directions with respect to the crystallographic axes of the sample. To study MQT rates we sweep the applied $z$-axis field at a constant rate ($\dot{\alpha} = dH_0/dt$) through a resonance and measure the change in sample magnetization, $M_{\text{before}} - M_{\text{after}}$ [22]. The normalized magnetization change $(M_{\text{before}} - M_{\text{after}})/(M_{\text{before}} - M_{\text{eq}})$, where $M_{\text{eq}}$ is the equilibrium magnetization, is the MQT probability, $P$. For a monodisperse system of molecules, this probability is related to the quantum splitting of the resonance, $\Delta$, through the Landau-Zener formula $P_{LZ} = 1 - \exp(-\pi \Delta^2/2v_0 \alpha)$, where $v_0 = g \mu_B (2S - k)$ and $v_0 \alpha$ is the energy sweep rate. When there is a distribution of quantum splittings in a crystal this situation changes. Now the MQT probability depends on the distribution of tunnel splittings of the molecules in the initial state $m = 10$ (the metastable state) prior to crossing the resonance. Therefore, it is possible to study different parts of the distribution (such as molecules with either the largest or smallest tunnel splittings) by appropriate preparation of the initial magnetization state, as will be described below.

In our first experiments, two different magnetization states were studied. In the first case (a) $M_{\text{initial}} = M_z$ and we study relaxation with the field applied along the $-z$ direction ($M_{\text{eq}} = -M_z$). The initial state corresponds to all molecules in the state $m = 10$ and the entire distribution of quantum splittings (100%) contributes to the relaxation as the field is increased along the $-z$ direction. Note that for the smallest observable resonances the molecules with the largest tunnel splittings within this distribution will make the dominant contribution. In the second case, (b), we start with $M_{\text{initial}} = -0.4M_z$, having allowed 70% of the molecules to relax prior to the experiment by crossing resonance $k = 6$ (in the absence of an applied transverse field). We are thus examining 30% of the molecules with smallest tunneling splittings. After we prepare these magnetic states we sweep the longitudinal magnetic field at a constant sweep rate ($\dot{\alpha} = 0.4 \text{T/min}$) from 0 T to about 5 T, while a transverse field of 0.4 T is applied at an angle, $\phi$, with respect to one of the faces of the crystal. We repeat this procedure for angles from $\phi = 0^\circ$ to $\phi = 360^\circ$.

In Fig. 1 we show the angular dependence of the MQT relaxation probability for both initial configurations. Resonance $k = 6$ is shown for case (a) and $k = 7$ for case (b). In both cases the result is a fourfold pattern of maxima in the MQT probability at $\phi = 60^\circ$, $150^\circ$, $240^\circ$, and $330^\circ$. There is also a onefold contribution due to a small misalignment between the applied field and the $z$ axis of the crystal which is represented by a continuous line in the figure. It is clear that both initial magnetization states show the same behavior for the probability versus angle of the transverse field. Since these initial configurations represent two different parts of the tunnel splittings distribution (high and low ends of the distribution), this indicates that the fourfold symmetry of the MQT probability is a property of a significant fraction of the molecules in the crystal. This fourfold rotation pattern is qualitatively consistent with the fourth order transverse anisotropy term in the Hamiltonian of Eq. (1). Note that this term leads to two hard and two medium magnetic axes in the $x$-$y$ plane. For example, for positive $C$ the $x$ and $y$ ($\phi = n \pi/2$, with $n = 0, 1, 2, 3$) axes are hard and $x = \pm y$ ($\phi = (2n + 1) \pi/2$) are medium axes. A magnetic field applied parallel to a medium magnetic axis produces a larger tunnel splitting than the same field applied along a hard axis [23]. However, the value of the parameter $C$ found by EPR spectroscopy, $\sim 3 \times 10^{-5}$ K, would produce a change in tunneling probability of only $\sim 15\%$, much smaller than the results observed in the lower curve in Fig. 1.

In order to determine the origin of this fourfold symmetry and whether it is intrinsic to the Mn$_{12}$ molecule, we have conducted the following experiment. We have selected a fraction of molecules in the crystal by applying a selection transverse field (STF), $H_{\text{STF}} = 0.6$ T, aligned with one of the maxima in Fig. 1, i.e., parallel to a medium magnetic axis, while crossing resonance $k$, with the longitudinal field swept along $+z$. Then we study this fraction of molecules; we measure the magnetization versus longitudinal with the field swept in the opposite direction, along $-z$, in the presence of a transverse field of 0.3 T applied at different angles, $\phi$, as was done in Fig. 1. First, the STF was set at $\phi_{\text{select}} = 60^\circ$ and in

![FIG. 1. MQT relaxation probability versus the angle $\phi$ between the applied transverse magnetic field and one of the faces of the crystal for resonance $k = 6$ (with the whole crystal) and $k = 7$ (for 30% of the molecules with smallest tunnel splittings). The solid line represents the effect of misalignment between the longitudinal field and the easy axis of the crystal.]
separate experiments both 50% (selection with \( k = 6 \)) and 10% (selection with \( k = 5 \)) of molecules with the largest tunnel splitting were studied for this angle of the STF. The same procedure was repeated with the STF in a direction orthogonal to the first case (\( \phi_{\text{select}} = 150^\circ \)), with 50% of molecules with the largest tunnel splittings. The behavior of the MQT probability versus the angle, \( \phi \), is shown in Fig. 2 for resonance \( k = 6 \) and for the three initial magnetization states described above. The results in all the cases show a twofold rotation pattern of the MQT probability, in clear contrast with the fourfold rotation pattern observed when there was no transverse field used to select the initial state of the sample. When the STF was applied at \( \phi_{\text{select}} = 60^\circ \) (left figure), the results show only two maxima at 60° and 240°. On the other hand, for the selection at \( \phi_{\text{select}} = 150^\circ \) the probability shows maxima at 150° and 330°. In the left polar plot in Fig. 2 we show the results for both angle selections, \( \phi_{\text{select}} = 60^\circ \) (solid circles) and \( \phi_{\text{select}} = 150^\circ \) (open circles), where the effect of the field misalignment has been corrected.

The observation of a twofold symmetry in the MQT relaxation probability, with a 90° phase difference that depends on the direction of the STF, is clear evidence that molecules in the crystal have lower than fourfold symmetry. These observations are in excellent accord with the isomer model of Cornia et al. [15]. There are six isomers in this model, four of which have lower symmetry than tetragonal (and comprise about 90% of the molecules in the crystal) and thus have a second-order transverse magnetic anisotropy, \( E(S_x^2 - S_y^2) \). This anisotropy gives rise to a twofold rotation symmetry for fields in the \( x-y \) plane, with maxima in the MQT probability separated by 180°. The maxima occur when the applied field is aligned with the medium magnetic axis (for \( E < 0 \) the \( x \) axis, and for \( E > 0 \) the \( y \) axis). Since the crystal has tetragonal symmetry there must be equal populations of isomers with opposite signs of \( E \). A change in the sign of \( E \) rotates the hard and medium axes of the molecule by 90°, explaining the average fourfold symmetry observed in the crystal (Fig. 1). Moreover, the isomers found in x-ray diffraction have their hard axes in the following directions: 50°–60°, 140°–150°, 230°–240°, and 320°–330° with respect to crystal faces [24], as we observe in Fig. 2. Importantly, this observation is not consistent with the dislocation model [14], since in this model the distribution of medium axes directions is isotropic, excluding very small regions of the crystal near the dislocation cores. The polar plot on the right in Fig. 2 shows the calculated tunnel splittings for resonance \( k = 6 \) versus \( \phi \). The solid thin line represents the angular dependence of the tunnel splitting for \( E = 0 \). An estimation of the magnitudes of \( E \) needed to explain the change in the MQT relaxation observed in Figs. 1 and 2 are \( E \sim 0.5 \text{ mK} \) (Fig. 1 upper curve, molecules with the smallest tunnel splittings), \( E \sim 2.5 \text{ mK} \) (Fig. 1 lower curve, the whole distribution), \( E \sim 2.5 \text{ mK} \) (Fig. 2, 50% of the largest tunnel splittings with transverse field selection), and \( E \sim 10 \text{ mK} \) (Fig. 2, 10% with the same transverse field selection). Recent EPR experiments suggest similar values of \( E \) [19].

By applying a STF in a given direction we can select molecules with a particular direction of their medium axes. We have thus selected molecules with their medium axis along \( \phi_{\text{select}} = 60^\circ \), and 10% and 50% of the distribution of such molecules, for further investigation (as in Fig. 2 on left). We have studied the MQT relaxation as a function of the magnitude of the transverse field applied along both the hard (\( \phi = 150^\circ \)) and medium (\( \phi = 60^\circ \)) axes of such molecules. The results for resonances \( k = 5 \), 6, and 7 are shown in Fig. 3. The probability is plotted on a logarithmic scale versus the transverse magnetic field. For a given resonance, the difference between these orientations of the transverse field is clearly larger in the experiment with 10% of the molecules (biggest splittings) than with 50%. This indicates that the average value of the second-order transverse anisotropy increases as we select the largest tunnel splittings in the distribution. An estimation gives average \( E \) values of \( E(50\%) \sim 2.5 \text{ mK} \), \( E(10\%) \sim 10 \text{ mK} \). These are the same values as those extracted from the change of the probability in the rotation experiments. One significant difference in the transverse field dependence of the probability can be observed through the comparison of the graphics in Fig. 3. In the results for 50% of the distribution, the probability increases exponentially for both transverse field orientations. However, in the experiment with 10% of the molecules the MQT relaxation probability deviates significantly from exponential behavior, showing the largest deviations at fields \( H_p(k = 5) \sim 0.45 \text{ T}, H_p(k = 6) \sim 0.3 \text{ T}, \)
and \( H_p(k = 7) \approx 0.35 \) T. This is reminiscent of the Berry phase observed in the SMM Fe\(_8\) [22]. The modeling that we have carried out using the values of \( E \) extracted from our data gives minima in the tunneling probability for \( H_{\text{min}}(k = 5) \approx 0 \) and 0.5 T, \( H_{\text{min}}(k = 6) \approx 0.25 \) T, and \( H_{\text{min}}(k = 7) \approx 0 \) and 0.6 T. Some of these minima occur where we observe plateaus in Fig. 3. The distribution of \( E \) values in the experiment probably smooths the minima leading to the plateaus we observe. On the other hand, the measured MQT probability does not show parity effects for the resonances at zero transverse field. In the absence of transverse fields, the symmetry breaking terms in the Hamiltonian are due to the transverse anisotropy of the molecules. Fourth order transverse anisotropy only allows tunneling transitions for resonances \( k \) that are a multiple of 4 (\( k = 4i \)), while second-order anisotropy only allows transitions for \( k \) a multiple of 2 (\( k = 2i \)).

The observation of tunneling relaxation at odd resonances must be due to the presence of local transverse fields. In the Cornia model this is explained naturally as small tilts of the molecular axis of the isomers. Other possibilities include transverse dipolar and nuclear fields or dislocations.

In summary, the average fourfold symmetry of MQT in Mn\(_{12}\)-acetate is due to equal populations of isomers with biaxial anisotropy that have orthogonal medium magnetic axes. Measurements of the tunneling probability versus transverse field show evidence for Berry phase effects probably due to a combination of second and fourth order transverse magnetic anisotropies. From a broader perspective, these results illustrate how subtle changes in molecule environment can modulate magnetic anisotropy and magnetic quantum tunneling. This sensitivity to local chemical environments is likely to be general to magnetism in molecules and ultimately useful in controlling their quantum properties.

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[20] Deuterated crystals were studied because the purity of the chemicals used in the synthesis leads to very high quality crystals. The hydrogen bonding framework is the same as that of H-Mn\(_{12}\), while minor changes in the hydrogen bonding interactions are expected.
[23] For fields parallel to the hard axis Berry phase oscillations are expected [22], leading to “zeros” in the tunnel splitting at certain fields. This would further increase the difference between the tunneling rates for medium and hard axes magnetic fields. Such significant changes in the rates for different field directions are not observed (see Fig. 3).